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tank circuit resonance frequency f of circuit tuning filtering calculator A Radio Frequency (RF) tank circuit is a fundamental component used in RF electronic circuits for tuning and filtering purposes. It consists of inductors (L) and capacitors (C) arranged in a specific configuration to resonate at a particular frequency. Explore the tank circuit calculator and learn about LC tank circuit basics and its resonant frequency formula. In an RF tank circuit, the inductor and capacitor are often connected in parallel or in series. The RF signal to be tuned or filtered is applied to this tank circuit. When the frequency of the input signal matches the resonance frequency of the tank circuit, it becomes highly reactive, and the impedance of the tank circuit becomes maximum. This means the circuit will absorb maximum energy from the input signal at that frequency. LC Tank Circuit Examples Here are a couple of examples demonstrating how the LC tank circuit calculator works: EXAMPLE #1: INPUTS: L = 10e-3 Henrys (i.e. 10mH) C = 100e-6 Farads (i.e. 100 F) OUTPUT: Tank circuit resonance frequency (Fr) = 0.0001591 MHz or 159.15 Hz. EXAMPLE #2: INPUTS: L = 100 Henrys C = 10 Farads OUTPUT: Fr = 5.03e-9 HzFr = 0.00503 Hz Applications of RF Tank Circuits RF tank circuits have numerous applications, including: Tuning Circuit: RF tank circuits are used in tuning circuits of radios, televisions, and transmitters. By adjusting the values of the inductor or capacitor, the resonant frequency can be changed, allowing the circuit to be tuned. Filtering: RF tank circuits can be used as bandpass or band-stop filters in RF systems, allowing specific frequencies to pass through while attenuating others. Resonant Frequency Formula for LC Tank Circuits When an inductor and a capacitor are connected in parallel or in series, they form a resonant circuit. This resonant circuit can store energy at a specific frequency. The resonance frequency is determined by the values of the inductor and capacitor. The following resonant frequency formula is used in this calculator to calculate the resonance frequency of an LC tank circuit: In the equation, Fr is the resonant frequency in Hertz (Hz), L is the inductance in Henry (H), and C is the capacitance in Farad (F). pi is a mathematical constant (Approximately 3.14159). Conclusion Overall, RF tank circuits play a crucial role in RF circuit design, enabling tuning and filtering of signals at specific frequencies. They are essential components in various RF systems, including communication devices, transmitters, receivers, and antennas. There are other types of tank circuits in electronics, each serving different purposes. The popular among them are audio tank circuit, Tesla Coil tank circuit, MRI (Magnetic Resonance Imaging) tank circuit, LC oscillator tank circuit, LC filter tank circuit, and RL tank circuit. A condition of resonance will be experienced in a tank circuit (Figure below) when the reactances of the capacitor and inductor are equal to each other. Because inductive reactance increases with increasing frequency and capacitive reactance decreases with increasing frequency, there will only be one frequency where these two reactances will be equal. Simple parallel resonant circuit (tank circuit). In the above circuit, we have a 10 F capacitor and a 100 mH inductor. Since we know the equations for determining the reactance of each at a given frequency, and we're looking for that point where the two reactances are equal to each other, we can set the two reactance formulae equal to each other and solve for frequency algebraically. So there we have it: a formula to tell us the resonant frequency of a tank circuit, given the values of inductance (L) in Henrys and capacitance (C) in Farads. Plugging in the values of L and C in our example circuit, we arrive at a resonant frequency of 159.155 Hz. What happens at resonance is quite interesting. With capacitive and inductive reactances equal to each other, the total impedance increases to infinity, meaning that the tank circuit draws no current from the AC power source! We can calculate the individual impedances of the 10 F capacitor and the 100 mH inductor and work through the parallel impedance formula to demonstrate this mathematically. As you might have guessed, I chose these component values to give resonance impedances that were easy to work with (100V even). Now, we use the parallel impedance formula to see what happens to total Z. We can't divide any number by zero and arrive at a meaningful result, but we can say that the result approaches a value off into the distance as the two parallel impedances get closer to each other. This means in practical terms that is that, the total impedance of a tank circuit is infinite (behaving as an open circuit) at resonance. We can plot the consequences of this with a power supply frequency range with a short SPICE simulation (Figure below) Resonant circuit suitable for SPICE simulation. freq (v1) 3.162E-04 1.000E-03 3.162E-03 1.0E-02 . . . . . 1.000E 02 9.632E-03 . . . . . 1.053E 02 8.506E-03 . . . . . 1.105E 02 7.455E-03 . . . . . 1.158E 02 6.470E-03 . . . . . 1.211E 02 5.542E-03 . . . . . 1.263E 02 4.663E-03 . . . . . 1.316E 02 3.828E-03 . . . . . 1.368E 02 3.033E-03 . . . . . 1.421E 02 2.271E-03 . . . . . 1.474E 02 1.540E-03 . . . . . 1.526E 02 8.373E-04 . . . . . 1.579E 02 1.590E-04 . . . . . 1.632E 02 2.969E-04 . . . . . 1.684E 02 1.132E-03 . . . . . 1.737E 02 1.749E-03 . . . . . 1.789E 02 2.350E-03 . . . . . 1.842E 02 2.934E-03 . . . . . 1.895E 02 3.505E-03 . . . . . 1.947E 02 4.063E-03 . . . . . 2.000E 02 4.609E-03 . . . . . tank circuit frequency sweep v1 0 ac 1 sin c 1 10 10u r hogs is necessary to eliminate a direct loop \* between v1 and I1, which SPICE can't handle bgsr 1 2 1e-121 2 0 100m ac lin 20 100 200 plot ac i v1 .end The 1 pico-ohm (1 p) resistor is placed in this SPICE analysis to overcome a limitation of SPICE: namely, that it cannot analyze a circuit containing a direct inductor-voltage source loop. (Figure below) A very low resistance value was chosen so as to have minimal effect on circuit behavior. This SPICE simulation plots circuit current over a frequency range of 10 to 200 Hz in twenty even steps (100 and 200 Hz inclusive). Current magnitude on the graph increases from left to right, while frequency increases from top to bottom. The current in this circuit takes a sharp dip around the analysis point of 157.9 Hz, which is the closest analysis point to our predicted resonance frequency of 159.155 Hz. It is at this point that total current from the power source falls to zero. The plot above is produced from the above spice circuit file (\*cir), the command (plot) in the last line producing the text plot on any printer or terminal. A better looking plot is produced by the nutmeg graphical post-processor, part of the spice package. The above spice (\*cir) does not use the plot (plot) command, though it does no harm. The following command will produce the plot below: (figure below) spice -b r resonant.cir -batch mode -r raw file, input is resonant.cir, nutmeg resonant.raw from the nutmeg prompt -> set plot ac 1 (set plot {enter} for list of plots) -display (for list of signals) -p mag (for magnitude) -complex current vector v1 #branch) Nutmeg produces plot of current (I1) for parallel resonant circuit. (Incidentally, the graph output produced by this SPICE computer analysis is more generally known as a Bode plot. Such graphs plot amplitude or phase shift on one axis and frequency on the other. The steepness of a Bode plot curve characterizes a circuit's frequency response, or how sensitive it is to changes in frequency. REVIEW: Resonance occurs when capacitive and inductive reactances are equal to each other. For a tank circuit with no resistance (R), resonant frequency can be calculated with the following formula: The total impedance of a parallel LC circuit approaches infinity as the power supply frequency approaches resonance. A Bode plot is a graph plotting waveform amplitude or phase on one axis and frequency on the other. A tank circuit achieves resonance when the reactances of the inductor and the capacitor balance out, maximizing the circuit's impedance and thus its efficiency at a specific frequency known as the resonant frequency (fr). The Tank Circuit Resonance Calculator is designed to compute this frequency based on the inductance (L) and capacitance (C) values provided, offering a quick, reliable means to enhance circuit performance. The fundamental formula the calculator uses is: Where fr is the resonant frequency in Hertz (Hz), L is the inductance in Henrys (H), and C is the capacitance in Farads (F). See also Portable Power Station Calculator Online This formula is derived from the principles of LC circuits where the inductive and capacitive reactances equate, leading to the peak impedance at the resonant frequency. Inductance (L) Capacitance (C) Resonant Frequency (fr) 10 mH 100 pF 159.155 kHz mH 100 pF 159.155 kHz 10 H 100 nF 503.3 kHz This table provides typical inductance and capacitance values along with their corresponding resonant frequencies, enabling users to estimate the frequency without performing calculations manually. To illustrate, lets calculate the resonant frequency for an inductor of 1 mH and a capacitor of 1 nF. See also Volts to Joules Calculator On Off = 1 (2 \* pi \* sqrt(1 + 10^-9) 159.155 kHz) This example shows how changing L and C values impacts fr, providing insights into tuning the circuit's performance. What is a tank circuit? A tank circuit consists of an inductor and a capacitor connected either in series or parallel, used primarily to filter signals at its resonant frequency. Why is the resonant frequency important? The resonant frequency determines where the circuit will be an efficiently filter or amplify signals. Crucial in applications like radio transmitters and audio electronics. By Jitender Singh on Feb 02, 2023 An LC circuit, also known as a resonant circuit or tank circuit, consists of an inductor (L) and a capacitor (C). It is a resonant circuit with a resonance frequency. When the energy oscillates between the inductor and the capacitor at the resonant frequency. At the resonant frequency, the reactance of the inductor and the capacitor cancel each other out, allowing a maximum transfer of energy between the two components. The charge q on the capacitor follows the differential equation (SHM) begin{aligned} \frac{d^2q}{dt^2} + \frac{q}{LC} = 0 \end{aligned} If initial charge on the capacitor is q\_0, then its variation with time is given by q = q\_0 \cos(\omega t). The current in the circuit is i = \frac{dq}{dt} = -q\_0 \omega \sin(\omega t). The electric field energy in the capacitor varies with time as E = \frac{1}{2} C V^2 = \frac{1}{2} C q^2 = \frac{1}{2} C q\_0^2 \cos^2(\omega t). The magnetic field energy in the inductor varies with time as W = \frac{1}{2} L I^2 = \frac{1}{2} L \left( \frac{dq}{dt} \right)^2 = \frac{1}{2} L \omega^2 q\_0^2 \sin^2(\omega t). Problems from IIT JEE Problem (IIT JEE 1998): An inductor of inductance 2.0 mH is connected across a charged capacitor of capacitance 5.0 \mu\text{mF} and the resulting LC circuit is set oscillating at its natural frequency. Let Q denote the instantaneous charge on the capacitor and i the current in the circuit. It is found that the maximum value of Q is 200 \mu\text{mC}. When Q = 100 \mu\text{mC}, what is the value of i? When Q = 200 \mu\text{mC}, what is the value of i? Find the maximum value of i. When i is equal to one-half of its maximum value, what is the value of Q? Solution: The charge in LC circuit oscillates with an angular frequency \omega = \frac{1}{\sqrt{LC}}. The energy of the system is conserved. i.e. \frac{1}{2} C Q^2 + \frac{1}{2} L I^2 = \frac{1}{2} C Q\_0^2 = \text{constant} Substitute Q = 200 \mu\text{mC} in the above equation to get \frac{1}{2} C (200 \mu\text{mC})^2 = \frac{1}{2} C Q^2 + \frac{1}{2} L I^2. Substitute this in the other equation to get \frac{1}{2} C (200 \mu\text{mC})^2 = \frac{1}{2} C Q^2 + \frac{1}{2} L I^2. Simplify to get i = \frac{Q\_0 \omega}{L} = \frac{200 \times 10^{-6} \times \frac{1}{\sqrt{2 \times 10^{-3} \times 5 \times 10^{-6}}}}{2 \times 10^{-3}} = 1.59 \text{ A} = 159 \text{ mA} \end{aligned} Related Alternating Current RC Circuit LR Circuit LCR Circuit Tank circuit resonance calculator The tank circuits are the combination of the capacitor (which is indicated as C) and inductor (which is indicated as L) which are connected parallel is called tank circuit. Tank circuit is also working as a resonance frequency. Formula Resonance frequency fr in Hz is equals to Reciprocal of 6.28 times of square root of product of inductance LH in ohms and the Capacitance CF in Farad. The formula for finding resonance frequency can be written as, Where fr = Resonant frequency in HzL = Inductance in HenryC = Capacitance in Farad = Having a constant value of 3.141592654 is Henry and Farad are the large units Example: Lets calculate resonant frequency by using tank circuit. Lets consider inductor L as 25 millihenries and capacitance C as 30 microfarads. Lets apply formula fr = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{25 \times 10^{-3} \times 30 \times 10^{-6}}} = 0.18377298 \text{ kHz} Learn More: Capacitive Current Calculator, Formula, Capacitive Calculation Share copy and redistribute the material in any medium or format for any purpose, even commercially. Adapt, remix, transform, and build upon the material for any purpose, even commercially. The licensor cannot revoke these freedoms as long as you follow the license terms. Attribution You must give appropriate credit, provide a link to the license, and indicate if changes were made. You may do so in any reasonable manner, but not in any way that suggests the licensor endorses you or your use. ShareAlike If you remix, transform, or build upon the material, you must distribute your contributions under the same license as the original. No additional restrictions You may not apply legal terms or technological measures that legally restrict others from doing anything the license permits. You do not have to comply with the license for elements of the material in the public domain or where your use is permitted by an applicable exception or limitation. No warranties are given. The license may not give you all of the permissions necessary for your intended use. For example, other rights such as publicity, privacy, or moral rights may limit how you use the material. Electrical "resonator" circuit, consisting of inductive and capacitive elements with no resistance This article needs additional citations for verification. Please help improve this article by adding citations to reliable sources. Unsourced material may be challenged and removed. Find sources: LC circuit news newspapers books scholar JSTOR (March 2009) (Learn how and when to remove this message) LC circuit diagram Linear analog electronic filters Network synthesis filters Butterworth filter Chebyshev filter Elliptic (Cauer) filter Bessel filter Gaussian filter Optimum "L" (Legendre) filter Linkwitz-Riley filter Image inductance filters Constant k filter - derived filter General image filters Zobel network (constant R) filter Lattice filter (all-pass) Bridged T delay equaliser (all-pass) Composite image filter m-type filter Simple filters RC filter RL filter LC filter V filter LC circuit are used either for generating signals at a particular frequency, or picking out a signal at a particular frequency from a more complex signal; this function is called a bandpass filter. They are key components in many electronic devices, particularly radio equipment, used in circuits such as oscillators, filters, tuners and frequency mixers. An LC circuit is an idealized model since it assumes there is no dissipation of energy due to resistance. Any practical implementation of an LC circuit will always include loss resulting from small but non-zero resistance within the components and connecting wires. The purpose of an LC circuit is usually to oscillate with minimal damping, so the resistance is made as low as possible. While no practical circuit is without losses, it is nonetheless instructive to study this ideal form of the circuit to gain understanding and physical intuition. For a circuit model incorporating resistance, see RLC circuit. The two-element LC circuit described above is the simplest type of inductor-capacitor network (or LC network). It is also referred to as a second order LC circuit [1][2] to distinguish it from more complicated (higher order) LC networks with more inductors and capacitors. Such LC networks with more than two reactances may have more than one resonant frequency. The order of the network is the order of the rational function describing the network in the complex frequency variable s. Generally, the order is equal to the number of L and C elements in the circuit and in any event cannot exceed this number. Animated diagram showing the operation of a tuned circuit (LC circuit). The capacitor C stores energy in its electric field E and the inductor L stores energy in its magnetic field B (green). The animation shows the circuit at progressive points in the oscillation. The oscillations are slowed down, in an actual tank circuit the charge may oscillate back and forth thousands to billions of times per second. An LC circuit, oscillating at its natural resonant frequency, can store electrical energy. See the animation. A capacitor stores energy in the electric field (E) between its plates, depending on the voltage across it, and an inductor stores energy in its magnetic field (B), depending on the current through it. If an inductor is connected across a charged capacitor, the voltage across the capacitor will drive a current through the inductor, building up a magnetic field around it. The voltage across the capacitor falls to zero as the charge is used up by the current flow. At this point, the energy stored in the coil's magnetic field induces a voltage across the coil, because inductors oppose changes in current. This induced voltage causes a current to begin to recharge the capacitor with a voltage of opposite polarity to its original charge. Due to Faraday's law, the EMF which drives the current is caused by a decrease in the magnetic field, thus the energy required to charge the capacitor is extracted from the magnetic field. When the magnetic field is completely dissipated the current will stop and the charge will again be stored in the capacitor, with the opposite polarity as before. Then the cycle will begin again, with the current flowing in the opposite direction through the inductor. The charge flows back and forth between the plates of the capacitor, through the inductor. The energy oscillates back and forth between the capacitor and the inductor until (if not replenished from an external circuit) internal resistance makes the oscillations die out. The tuned circuit's action, known mathematically as a harmonic oscillator, is similar to a pendulum swinging back and forth, or water sloshing back and forth in a tank; for this reason the circuit is also called a tank circuit.[3] The natural frequency (that is, the frequency at which it will oscillate when isolated from any other system, as described above) is determined by the capacitance and inductance values. In most applications the tuned circuit is part of a larger circuit which applies alternating current to it, driving continuous oscillations. If the frequency of the applied current is the circuit's natural resonant frequency (natural frequency f\_0) below, resonance will occur, and a small driving current can excite a large amplitude oscillating voltages and currents. In typical tuned circuits in electronic equipment the oscillations are very fast, from thousands to billions of times per second. [citation needed] Resonance occurs when an LC circuit is driven from an external source at an angular frequency \omega at which the inductive and capacitive reactances are equal in magnitude. The frequency at which this equality holds for the particular circuit is called the resonant frequency. The resonant frequency of the LC circuit is \omega = 1 / LC. (displaysyle omega\_0 = \frac{1}{\sqrt{LC}}) where L is the inductance in henries, and C is the capacitance in farads. The angular frequency \omega has units of radians per second. The equivalent frequency in units of hertz is f\_0 = \omega / 2\pi = 1 / 2\pi LC. (displaysyle f\_0 = \frac{\omega}{2\pi} = \frac{1}{2\pi\sqrt{LC}}) Output tuned circuit of shortwave radio transmitter from 1938 LC circuit (left) consisting of ferrite coil and capacitor used as a tuned circuit in the receiver for a radio clock The resonance effect of the LC circuit has many important applications in signal processing and communications systems. The most common application of tank circuits is tuning radio transmitters and receivers. For example, when tuning a radio to a particular station, the LC circuits are set at resonance for that particular carrier frequency. A series resonant circuit provides voltage magnification. A parallel resonant circuit can be used as load impedance in output circuits of RF amplifiers. Due to high impedance, the gain of amplifier is maximum at resonant frequency. Both parallel and series resonant circuits are used in induction heating. LC circuits behave as electronic resonators, which are a key component in many applications: Amplifiers Oscillators Filters Tuners Mixers Foster Seeley discriminator Contactless cards Graphics tablets Electronic article surveillance (security tags) By Kirchhoff's voltage law, the voltage VC across the capacitor and the voltage VL across the inductor must equal zero: VC + VL = 0. (displaysyle V\_C + V\_L = 0) Likewise, by Kirchhoff's current law, the current through the capacitor equals the current through the inductor: IC = IL. (displaysyle I\_C = I\_L) From the constitutive relations for the circuit elements, we also know that V\_L(t) = L \frac{dI\_L}{dt}, I\_C(t) = C \frac{dV\_C}{dt}. (displaysyle V\_L = L \frac{dI\_C}{dt}, I\_C = C \frac{dV\_C}{dt}) Rearranging and substituting the second order differential equation d^2 I + \omega^2 I = 0. (displaysyle \frac{d^2 I}{dt^2} + \omega^2 I = 0) Inductive reactance X\_L = L \omega. (displaysyle X\_L = L \omega) Capacitive reactance X\_C = \frac{1}{C \omega}. (displaysyle X\_C = \frac{1}{C \omega}) The parameter Q, the resonant angular frequency \omega\_0, is defined as \omega\_0 = 1 / LC. (displaysyle omega\_0 = \frac{1}{\sqrt{LC}}) Using this can simplify the differential equations: d^2 I + 2 \zeta \omega\_0 \frac{dI}{dt} + \omega\_0^2 I = 0. (displaysyle \frac{d^2 I}{dt^2} + 2 \zeta \omega\_0 \frac{dI}{dt} + \omega\_0^2 I = 0) The associated Laplace transform is s^2 + 2 \zeta \omega\_0 s + \omega\_0^2 = 0. (displaysyle s^2 + 2 \zeta \omega\_0 s + \omega\_0^2 = 0), thus s = -\zeta \omega\_0 \pm j \omega\_0 \sqrt{1 - \zeta^2}. (displaysyle s = -\zeta \omega\_0 \pm j \omega\_0 \sqrt{1 - \zeta^2}) where j is the imaginary unit. Thus, the complete solution to the differential equation is I(t) = A e^{s\_1 t} + B e^{s\_2 t} (displaysyle I(t) = A e^{s\_1 t} + B e^{s\_2 t}) and can be solved for A and B by considering the initial conditions. Since the exponential is complex, the solution represents a sinusoidal alternating current. Since the electric current I is a physical quantity, it must be real-valued. As a result, it can be shown that the constants A and B must be complex conjugates: A = B^\*. (displaysyle A = B^\*) Now let A = 10 e^{j\theta}. (displaysyle A = 10 e^{j\theta}) (displaysyle A = \frac{1}{\sqrt{2}} (I\_0 \cos(\theta) + j I\_0 \sin(\theta))) Therefore, B = 10 e^{-j\theta}. (displaysyle B = \frac{1}{\sqrt{2}} (I\_0 \cos(\theta) - j I\_0 \sin(\theta))) Next, we can use Euler's formula to obtain a real sinusoid with amplitude I\_0, angular frequency \omega = 1/LC, and phase angle (\theta). Thus, the resulting solution becomes I(t) = I\_0 \cos(\omega t + \theta). (displaysyle I(t) = I\_0 \cos(\omega t + \theta)) The initial conditions that would satisfy this result are I(0) = I\_0 \cos \theta. (displaysyle I(0) = I\_0 \cos \theta) V\_L(0) = L \frac{dI}{dt} \Big|\_{t=0} = 0 = L I\_0 \omega \sin \theta. (displaysyle V\_L(0) = L I\_0 \omega \sin \theta) Series LC circuit in the series configuration of the LC circuit, the inductor (L) and capacitor (C) are connected in series, as shown here. The total voltage V across the open terminals is simply the sum of the voltage across the capacitor, the voltage across the inductor, and the voltage across the inductor: V = V\_C + V\_L. I = I\_C = I\_L = I. (displaysyle V = V\_C + V\_L, I = I\_C = I\_L = I) Inductive impedance Z\_L = j\omega L. (displaysyle Z\_L = j\omega L) Capacitive impedance Z\_C = -j/\omega C. (displaysyle Z\_C = -j/\omega C) Inductive reactance X\_L = L \omega. (displaysyle X\_L = L \omega) Capacitive reactance X\_C = 1/C \omega. (displaysyle X\_C = \frac{1}{C \omega}) The parameter Q, the resonant angular frequency \omega\_0, is defined as \omega\_0 = 1 / LC. (displaysyle omega\_0 = \frac{1}{\sqrt{LC}}) Using this can simplify the differential equations: d^2 I + 2 \zeta \omega\_0 \frac{dI}{dt} + \omega\_0^2 I = 0. 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